



# BOOKLET SERIES

14/04/2019

AFFIX PRESCRIBED RUBBER STAMP

CODE :DEF-03/2019

Test Topic : PAIR OF STRAIGHT LINE QUADRATIC EQUATION AND BINOMIAL THEOREM

## MATHEMATICS

ROLL NO. (In figure)

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OMR SERIAL NO.

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(Only in english)

OMR SERIAL NO. (In words).....

NAME OF THE CENTRE .....

TIME : 1 Hour

MM : 100

Signature of the invigilator

### IMPORTANT INSTRUCTIONS

- 1- The candidate will write his/her Roll No. only at the place provided for i.e. on the cover page and on answer sheet given and nowhere else.
- 2- Immediately on the receipt of the question booklet, the candidate all the pages and that on question is missing. If there is any discrepancy, it should be reported by the candidate to the invigilator within 10 minutes of issue of this question booklet without any discrepancy be obtained.

### vko' ; d funʒk

- 1- vH; Fkhz viuk vupedk doy vkoj.k i'B rFkk izu i qLrdk dsl kFk fn; sx, mRrj&i=d dsfufn'ZV LFkku ij fy [kx\$ vU; = dgha ughA
- 2- izu i qLrdk feyus ds mi jklr vH; Fkhz dks rjUr tkp dj l fuf'pr dj yuh pkfg, fd i qLrdk ea i j'si "B gsrFkk dkbz izu NW rksugha x; k gA ; fn dkbz fol xfr gsrks izu&i qLrdk feyus ds 10 feuV ds Hkh rj gh d{k fujh{k dks l fpr djuk pkfg, rFkk =qV jfgr nw jh i qLrdk iklr dj yuh pkfg, A

**Numer of Questions : 50**

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# SHUKLA SIR MATHS CLASSES

M.M. : 100

MATHS

TIME : 1 Hour

T.G.T / P.G.T

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Test Topic : PAIR OF STRAIGHT LINE, QUADRATIC EQUATION AND BINOMIAL THEOREM

- The equation  $ax^2 + by^2 + cx + cy = 0, c \neq 0$  represents a pair of straight lines, If :  
(a)  $a + b = 0$  (b)  $a + c = 0$  (c)  $b + c = 0$  (d) None of these
- The angle between the lines represented by  $x^2 - y^2 = 0$  is :  
(a)  $0^\circ$  (b)  $45^\circ$  (c)  $90^\circ$  (d)  $180^\circ$
- The equation  $3x^2 + 2hxy + 3y^2 = 0$  represents a pair of straight lines passing through the origin. The two lines are  
(a) real and distinct, if  $h^2 > 3$  (b) real and distinct, if  $h^2 > 9$   
(c) real and distinct, if  $h^2 = 0$  (d) real and distinct, if  $h^2 > 3$
- If  $ax^2 + 2hxy + by^2 + 2gx + 2fy + c = 0$  represents parallel lines, then :  
(a)  $hf = bg$  (b)  $h^2 = ag$  (c)  $a^2f = b^2g$  (d) None of these
- The equation  $8x^2 + 8xy + 2y^2 + 26x + 13y + 15 = 0$  represents a pair of straight lines. The distance between them is :  
(a)  $\frac{7}{\sqrt{5}}$  (b)  $\frac{7}{2\sqrt{5}}$  (c)  $\sqrt{\frac{7}{5}}$  (d) None of these
- Independent term in the expansion of  $\left(2x + \frac{3}{x}\right)^{12}$  is :  
(a) 165 (b) 265 (c) 65 (d) None of these
- The sum of coefficients in the expansion of  $(x + y)^n$  is 33554432 then greatest coefficient in the expansion is:  
(a)  ${}^{24}C_{12}$  (b)  ${}^{26}C_{13}$  (c)  ${}^{27}C_{13}$  (d)  ${}^{25}C_{12}$
- Let  $T_n$  be the no. of quadrilateral formed by using non collinear points and  $T_{n+1} - T_n = 56$ , then n will be :  
(a) 7 (b) 6 (c) 8 (d) 9
- The number of terms in the expansion of  $(3x + y + z + t)^{20}$  is :  
(a) 190 (b) 2100 (c) 25 (d) None of these
- The coefficient of 10th term from the last in the expansion of  $\left(3x^2 + \frac{5}{x}\right)^{65}$  is :  
(a) 21000 (b) 51502 (c) 15500 (d) None of these
- The pair of straight lines given by  $2x^2 + 3y^2 - 6xy + 2x - 3y + 5 = 0$  has only bisector as :  
(a)  $x - y = 0$  (b)  $x + y = 0$  (c)  $x - 2y = 0$  (d) none

12. The family of straight lines  $(2a + 3b)x + (a - b)y + 2a - 4b = 0$  is concurrent at the point :

- (a)  $\left(\frac{2}{5}, -\frac{14}{5}\right)$       (b)  $\left(\frac{-2}{5}, \frac{-14}{5}\right)$       (c)  $\left(-\frac{2}{5}, \frac{14}{5}\right)$       (d)  $\left(\frac{2}{5}, \frac{14}{5}\right)$

13. If  $m_1$  and  $m_2$  are the slopes of the lines represented by the equation  $ax^2 + 2hxy + by^2 = 0$ , then the value of  $m_1 + m_2$  is :

- (a)  $\frac{2h}{b}$       (b)  $-\frac{2h}{b}$       (c)  $\frac{2h}{a}$       (d)  $-\frac{2h}{a}$

14. The difference of the tangent of the angle which the lines  $x^2(\sec^2 \theta - \sin^2 \theta) - 2xy \tan \theta + y^2 \sin^2 \theta = 0$  make with x-axis is :

- (a)  $2 \tan \theta$       (b) 2      (c)  $2 \cot \theta$       (d)  $\sin 2\theta$

15. Which of the following pair of straight lines intersect at right angle?

- (a)  $2x^2 = y(x + 2y)$       (b)  $(x + y)^2 = x(y + 3x)$       (c)  $2y(x + y) = xy$       (d)  $y = \pm 2x$

16. The equation  $\frac{a}{x-a} + \frac{b}{x-b} = 1$  has roots equal in magnitude but opposite in sign, then the value of  $a + b$  is :

- (a) -1      (b) 0      (c) 1      (d) None of these

17. If  $a, b, p, q$  are non-zero numbers, then the two equations  $2a^2x^2 - 2abx + b^2 = 0$  and  $p^2x^2 + 3pqx + q^2 = 0$ , have :

- (a) no common root      (b) one common roots, iff  $2a^2 + b^2 = p^2 + q^2$   
 (c) two common roots, iff  $3pq = 2ab$       (d) two common roots, iff  $3qb = 2ap$

18. If  $a, b, c$  are real and the difference between the roots of the quadratic equation  $ax^2 + bx + c = 0$  is less than 2, then  $\Delta$ , the discriminant satisfies by the relation :

- (a)  $0 \leq \Delta < 4a^2$       (b)  $4a^2 < \Delta$       (c)  $\Delta = 4a^2$       (d) none of these

19. If  $a(p + q)^2 + 2bpq + c = 0$  and  $a(p + r)^2 + bpr + c = 0$  then  $qr$  equals :

- (a)  $p^2 + \frac{c}{a}$       (b)  $p^2 + \frac{a}{c}$       (c)  $p^2 + \frac{a}{b}$       (d)  $p^2 + \frac{b}{a}$

20. The number of real roots of the equation  $\left(x + \frac{1}{x}\right)^3 + \left(x + \frac{1}{x}\right) = 0$  is :

- (a) 2      (b) 0      (c) 1      (d) 3

21. The value of a for which one root of the equation  $x^2 = (a + 1)x + a^2 + a - 8 = 0$  exceeds 2 and the other is less than 2 are given by :

- (a)  $a > 3$       (b)  $0 < a < 10$       (c)  $-2 < a < 3$       (d) None of these

22. The equation  $(3 - x)^4 + (2 - x)^4 = (5 - 2x)^4$  has :

d two non-real roots (d) None

23. If  $\alpha$  and  $\beta$  are two roots of the quadratic equations  $x^2 + px + 1 = 0$  and  $\gamma, \delta$  are the roots of  $x^2 + qx + 1 = 0$ , then  $(a - \gamma)(\beta - \gamma)(\alpha + \delta)(\beta + \delta) =$ :
- (a)  $q^2 + p^2$  (b)  $q^2 - p^2$  (c)  $q^2 - 2p$  (d) None of these
24. If the equation  $x^4 - 8x^3 + ax^2 + bx + 16 = 0$  has positive roots, then  $(a, b)$  is :
- (a)  $(2, 4)$  (b)  $(16, -24)$  (c)  $(24, -32)$  (d)  $(32, -24)$
25. The value of 'a' for which  $(a^2 - 1)x^2 + 2(a - 1)x + 2$  is positive for any x are :
- (a)  $a \geq 1$  (b)  $a \leq 1$  (c)  $a \geq -3$  (d)  $a \leq -3$  or  $a \geq 1$
26. If  $b_1 b_2 = 2(c_1 + c_2)$ , then at least one of the equations  $x^2 + b_1 x + c_1$  and  $x^2 + b_2 x + c_2$  has :
- (a) real roots (b) purely imaginary roots (c) imaginary roots (d) none of these
27. Number of real solutions of the equation  $\sin a^x \cos a^x = \frac{a^x + a^{-x}}{4}$  is :
- (a) 1 (b) 2 (c) 3 (d) 0
28. The set of values of x, which satisfy  $5x + 2 < 3x + 8$  and  $\frac{x + 2}{x - 1} < 4$  is :
- (a)  $(2, 3)$  (b)  $(-\infty, 1) \cup (2, 3)$  (c)  $(-\infty, 1)$  (d)  $(1, 3)$
29. The condition that  $x^3 - px^2 + qx - r = 0$  may have two of its roots equal to each other but of opposite signs is :
- (a)  $r = pq$  (b)  $r = 2p^3 + pq$  (c)  $r = p^2 q$  (d) None of these
30. If  $\alpha$  is a roots of the equation  $x^{11} - x^{10} + x^8 - x^7 + x^5 - x^4 + x^2 - x - 20 = 0$  then  $\alpha^{12}$
- (a) is equal to 61 (b) is greater than 61 (c) is less than 61 (d) none of these
31. If  $\alpha$  and  $\beta$  are the roots of  $x^2 + x + 1 = 0$ , then  $2\alpha^{13} + 3\beta^{13}$  and  $3\alpha^{31} + 2\beta^{31}$  are the roots of :
- (a)  $x^2 - x + 1 = 0$  (b)  $x^2 + 5x + 7 = 0$  (c)  $x^2 - 5x - 7 = 0$  (d)  $x^2 + 5x - 7 = 0$
32. If  $a + b + c = 0$  then the roots of the equation  $3ax^2 + 4bx + 5c = 0$  are :
- (a) positive (b) negative (c) real and distinct (d) complex
33. The quadratic equation with real coefficients one of those complex roots has the real part 12 and modules 13 is :
- (a)  $x^2 - 12x + 13 = 0$  (b)  $x^2 - 24x + 13 = 0$  (c)  $x^2 - 24x + 169 = 0$  (d)  $x^2 - 24x - 169 = 0$
34. Solution of the equation  $\log_5 \left( 5^{\frac{1}{x}} + 125 \right) = \log_5 6 + \left( 1 + \frac{1}{2x} \right)$  is :
- (a)  $\{2, 4\}$  (b)  $\left\{ \frac{1}{2}, \frac{1}{4} \right\}$  (c)  $\left\{ 2, \frac{1}{4} \right\}$  (d)  $\left\{ \frac{1}{2}, 4 \right\}$
35. If x satisfies  $|x - 1| + |x - 2| + |x - 3| \geq 6$  then
- (a)  $x \leq x \leq 4$  (b)  $x \leq -2$  or  $x \geq 4$  (c)  $x \leq 0$  or  $x \geq 4$  (d) None of these

36. If  $\alpha$  and  $\beta$  are roots of the equation  $x^2 + px + q = 0$  and also of  $x^{2n} + p^n x^n + q^n = 0$ . If  $\frac{\alpha}{\beta}$  and  $\frac{\beta}{\alpha}$  are roots of  $(x+1)^n + x^n + 1 = 0$ , then  $n$  must be :
- (a) an even integer                      (b) an odd integer                      (c) equal to 2                      (d) none of these
37. The smallest +ve integer  $n$ , for which  $n! < \left(\frac{n+1}{2}\right)^n$  holds is :
- (a) 1                      (b) 2                      (c) 3                      (d) 4
38.  $2^{2n} - 7n - 1$  is divisible by
- (a) 36                      (b) 64                      (c) 49                      (d) 25
39. Coefficient of  $x^{-4}$  in  $\left(\frac{3}{2} - \frac{3}{x^2}\right)^{10}$  is :
- (a)  $\frac{405}{226}$                       (b)  $\frac{504}{259}$                       (c)  $\frac{450}{263}$                       (d) None of these
40. The number of dissimilar terms in the expansion of  $(a+b)^n$  is  $n+1$ , therefore number of dissimilar terms in the expansion of  $(a+b+c)^{12}$  is :
- (a) 13                      (b) 39                      (c) 78                      (d) 91
41. The power of  $x$  occurring in the 7th term in the expansion of  $\left(\frac{4x}{5} - \frac{8}{5x}\right)^9$  is :
- (a) 3                      (b) -3                      (c) 5                      (d) -5
42. Sum of the coefficient in the expansion of  $(ax^3 - 3x + 2)^{25}$  is equal to the sum of the coefficients in the expansions of  $(x^2 - ay^2)^{25}$ , then the value of  $a$  equals :
- (a) -1                      (b) 1                      (c) 0                      (d) none of these
43. In the expansion of  $(1+x)^{11}$  the fifth term is 24 times the third term. Then the value of  $x^2$  is :
- (a) 4                      (b) 9                      (c) 16                      (d) 24
44. Fifth term from the end in the expansion of  $\left(\frac{x^3}{2} - \frac{2}{x^2}\right)^{12}$  is :
- (a)  $-7920x^{-4}$                       (b)  $7920x^{-4}$                       (c)  $7920x^4$                       (d)  $-7920x^4$
45. The sum of the series  $\sum_{r=0}^{10} {}^{20}C_r$  is :
- (a)  $2^{20}$                       (b)  $2^{19}$                       (c)  $2^{19} + \frac{1}{2} {}^{20}C_{10}$                       (d)  $2^{10} - \frac{1}{2} {}^{20}C_{10}$

46. The coefficient of  $x^m$  in  $(1+x)^p + (1+x)^{p+1} + \dots + (1+x)^n$ ,  $p \leq m \leq n$  is :

- (a)  ${}^{n+1}C_{m+1}$                       (b)  ${}^{n-1}C_{m-1}$                       (c)  ${}^nC_m$                       (d)  ${}^nC_{m+1}$

47. If  $(1+x)^n = C_0 + C_1x + C_2x^2 + \dots + C_nx^n$ , then  $C_0^2 + C_1^2 + \dots + C_n^2$  is equal to :

- (a)  $2^n C_n$                       (b)  $2^n C_{n-1}$                       (c)  $2^{n+1} C_n$                       (d)  $2^{n-1} C_n$

48. The coefficient of  $x^{50}$  in the expansion  $(1+x)^{100} + 2x(1+x)^{99} + 3x^2(1+x)^{98} + \dots + 1001x^{1000}$  is :

- (a)  ${}^{100}C_{50}$                       (b)  ${}^{1001}C_{50}$                       (c)  ${}^{1002}C_{50}$                       (d)  ${}^{1000}C_{50}$

49. If  $n \in N$  such that  $(7 + 4\sqrt{3})^n = I + F$  where  $I \in N$  and  $0 < F < 1$ , then the value of  $(I + F)(I - F)$  is :

- (a) 0                      (b) 1                      (c)  $7^{2n}$                       (d)  $2^{2n}$

50. The sum of all the coefficients of the expansion of  $(x + y)^n$  is 1024. Then the greatest coefficient in the  $r$ th term, where  $r =$

- (a) 6                      (b) 5                      (c) 4                      (d) None

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SHUKLA SIR

14-04-2019

MATH TEST - ANSWERS									
TOPIC : STRAIGHT LINE AND COMPLEX NUMBER									
1.	2.	3.	4.	5.	6.	7.	8.	9.	10.
<i>a</i>	<i>c</i>	<i>b</i>	<i>a</i>	<i>b</i>	<i>d</i>	<i>d</i>	<i>c</i>	<i>d</i>	<i>d</i>
11.	12.	13.	14.	15.	16.	17.	18.	19.	20.
<i>d</i>	<i>a</i>	<i>b</i>	<i>b</i>	<i>a</i>	<i>b</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>b</i>
21.	22.	23.	24.	25.	26.	27.	28.	29.	30.
<i>c</i>	<i>c</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>a</i>	<i>d</i>	<i>b</i>	<i>a</i>	<i>b</i>
31.	32.	33.	34.	35.	36.	37.	38.	39.	40.
<i>b</i>	<i>c</i>	<i>c</i>	<i>b</i>	<i>c</i>	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>d</i>
41.	42.	43.	44.	45.	46.	47.	48.	49.	50.
<i>b</i>	<i>b</i>	<i>a</i>	<i>b</i>	<i>c</i>	<i>a</i>	<i>a</i>	<i>c</i>	<i>b</i>	<i>a</i>